

Research Article

Catalytic Mechanism of LENR in Quasicrystals based on Localized Anharmonic Vibrations and Phasons

V. Dubinko*

NSC “Kharkov Institute of Physics and Technology,” Kharkov, Ukraine

D. Laptev

B. Verkin Institute for Low Temperature Physics and Engineering, Kharkov, Ukraine

K. Irwin

Quantum Gravity Research, Los Angeles, USA

Abstract

Quasicrystals (QCs) are a novel form of matter, which are neither crystalline nor amorphous. Among many surprising properties of QCs is their high catalytic activity. We propose a mechanism explaining this peculiarity based on unusual dynamics of atoms at special sites in QCs, namely, localized anharmonic vibrations (LAVs) and phasons. With the vibrations, one deals with a large amplitude (\sim fractions of an angstrom) time-periodic oscillations of a small group of atoms around their stable positions in the lattice, known also as discrete breathers, which can be excited in regular crystals as well as in QCs. On the other hand, phasons are a specific property of QCs, which are represented by very large amplitude (\sim angstrom) oscillations of atoms between two quasi-stable positions determined by the geometry of a QC. Large amplitude atomic motion in LAVs and phasons results in time-periodic driving of adjacent potential wells occupied by hydrogen ions (protons or deuterons) in case of hydrogenated QCs. This driving may result in the increase of amplitude and energy of zero-point vibrations (ZPV). Based on that, we demonstrate a drastic increase of the D–D or D–H fusion rate with increasing number of modulation periods evaluated in the framework of Schwinger model, which takes into account the suppression of the Coulomb barrier due to lattice vibrations. In this context, we present a numerical solution of Schrodinger equation for a particle in a non-stationary double well potential, which is driven time-periodically imitating the action of a LAV or phason. We show that the rate of tunneling of the particle through the potential barrier separating the wells is drastically enhanced by the driving, and it increases strongly with increasing amplitude of the driving. These results support the concept of nuclear catalysis in QCs that can take place at special sites provided by their inherent topology. Experimental verification of this hypothesis can lead to new ways of engineering materials containing nuclear active environments based on QC catalytic properties. © 2017 ISCMNS. All rights reserved. ISSN 2227-3123

Keywords: Quasicrystals, Localized anharmonic vibrations, Low energy nuclear reactions, Nuclear active sites, Phasons, Tunneling

1. Introduction

The tunneling through the Coulomb potential barrier during the interaction of charged particles presents a major problem for the explanation of low energy nuclear reactions (LENR) observed in solids [1–3]. Corrections to the cross section of the fusion due to the screening effect of atomic electrons result in the so-called “screening potential,” which is far too weak to explain LENR observed at temperatures below the melting point of solids. Nobel laureate Julian Schwinger proposed that a substantial suppression of the Coulomb barrier may be possible at the expense of *lattice vibrations* [4,5]. The fusion rate of deuteron–deuteron or proton–deuteron oscillating in adjacent lattice sites of a metal hydride, according to the Schwinger model, is about 10^{-30} s^{-1} [6], which is huge as compared to the conventional evaluation by the Gamov tunnel factor ($\sim 10^{-2760}$). However, even this is too low to explain the observed excess heat generated, e.g. in Pd cathode under D_2O electrolysis. The fusion rate by Schwinger is extremely sensitive to the amplitude of *zero-point vibrations* (ZPV) of the interacting ions, which has been shown to increase under the action of time-periodic driving of the harmonic potential well width [6]. Such a driving can be realized in the vicinity of *localized anharmonic vibrations* (LAVs) defined as large amplitude (\sim fractions of an angstrom) time-periodic vibrations of a small group of atoms around their stable positions in the lattice. A sub-class of LAV, known as *discrete breathers*, can be excited in regular crystals by heating [1–3,7] or irradiation by fast particles [8]. Based on that, a drastic increase of the D–D or D–H fusion rate with increasing number of driving periods has been demonstrated in the framework of the modified Schwinger model [6,8].

One of the most important practical recommendations of the new LENR concept is to look for the *nuclear active environment* (NAE), which is enriched with nuclear active sites, such as the LAV sites. In this context, a striking *site selectiveness* of LAV formation in disordered structures [9] allows one to suggest that their concentration in quasicrystals (QCs) may be very high as compared to regular crystals where discrete breathers arise homogeneously, and their activation energy is relatively high. Direct experimental observations [10] have shown that in the decagonal quasicrystal $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$, *mean-square thermal vibration amplitude* of the atoms at special sites substantially exceeds the mean value, and the difference increases with temperature. This might be the first experimental observation of LAV, which has shown that they are arranged in just a few nanometers from each other, so that their average concentration was about 10^{20} per cubic cm that is many orders of magnitude higher than one could expect to find in periodic crystals [1–3,7]. Therefore, in this case, one deals with a kind of ‘*organized disorder*’ that stimulates formation of LAV, which may explain a strong catalytic activity of quasicrystals [11].

In addition to the enhanced susceptibility to the LAV generation, QCs exhibit unique dynamic patterns called *phasons*, which are represented by *very* large amplitude (\sim angstrom) quasi time-periodic oscillations of atoms between two quasi-stable positions determined by the geometry of a QC. It is natural to expect that the driving effect of phasons can exceed that of LAVs due to the larger oscillation amplitude in phasons. The main goal of the present paper is to develop this concept to the level of a quantitative comparison between the driving/catalytic action of LAVs and phasons, which could be used to suggest some practical ways of catalyzing LENR.

The paper is organized as follows. In the next section, the Schwinger model [4,5] and its extension [6] are shortly reviewed to demonstrate an importance of time-periodic driving of potential wells in the LENR triggering.

In Section 3, we extend our analysis beyond the model case of infinite harmonic potential (the tunneling from which is impossible) and obtain numerical solution of Schrödinger equation for a particle in a *non-stationary* double well potential, which is driven time-periodically imitating the action of a LAV or phason. We show that the rate of

*E-mail: xxx

tunneling of the particle through the potential barrier separating the wells is enhanced drastically by the driving, and it increases strongly with increasing amplitude of the driving. In Section 4, we present some examples of dynamic patterns in QCs and their clusters and discuss the ways of experimental verification of the proposed concept. The summary and outlook is given in Section 5.

2. Schwinger Model of LENR in an Atomic Lattice Modified with Account of Time-periodic Driving

According to Schwinger [4], the effective potential of the deuteron–deuteron (D–D) or proton–deuteron (P–D) interactions is modified due to averaging ${}_0\langle \rangle_0$ related to their *zero-point vibrations* (ZPV) in adjacent harmonic potential wells, where ${}_0\langle \rangle_0$ symbolizes the phonon vacuum state. This means that nuclei in the lattice act not like point-like charges, but rather (similar to electrons) they are “smeared out” due to quantum oscillations in the harmonic potential wells near the equilibrium positions. The resulting effective Coulomb interaction potential ${}_0\langle V_c(r) \rangle_0$ between a proton and a neighboring ion at a distance r can be written, according to [4] as

$${}_0\langle V_c(r) \rangle_0 = \frac{Ze^2}{r} \sqrt{\frac{2}{\pi}} \int_0^{r/\Lambda_0} dx \exp\left(-\frac{1}{2}x^2\right) \approx \begin{cases} r \gg \Lambda_0 : \frac{e^2}{r} \\ r \ll \Lambda_0 : \left(\frac{2}{\pi}\right)^{1/2} \frac{e^2}{\Lambda_0}, \end{cases} \quad (1)$$

where Z is the atomic number of the ion, e is the electron charge, $\Lambda_0 = (\hbar/2m\omega_0)^{1/2}$ is the ZPV amplitude, \hbar is the Plank constant, m is the proton mass, and ω_0 is the angular frequency of the harmonic potential. A typical value of $\Lambda_0 \sim 0.1 \text{ \AA}$, which means that the effective repulsion potential is saturated at approximately *several hundred eV* as compared to *several hundred keV* for the unscreened Coulomb interaction. Schwinger estimated the rate of fusion as the rate of transition out of the phonon vacuum state, which is reciprocal of the mean lifetime T_0 of the vacuum state, which can be expressed via the main nuclear and atomic parameters of the system [5,6]:

$$\frac{1}{T_0} \approx 2\pi\omega_0 \left(\frac{2\pi\hbar\omega_0}{E_{\text{nucl}}}\right)^{1/2} \left(\frac{r_{\text{nucl}}}{\Lambda_0}\right)^3 \exp\left[-\frac{1}{2}\left(\frac{R_0}{\Lambda_0}\right)^2\right], \quad (2)$$

where E_{nucl} is the nuclear energy released in the fusion, which is transferred to the lattice producing phonons (*that explains the absence of harmful radiation in LENR*), r_{nucl} is the nuclear radius, R_0 is the equilibrium distance between the nuclei in the lattice.

For D–D $\Rightarrow \text{He}^4$ fusion in PdD lattice, the mass difference $E_{\text{nucl}} = 23.8 \text{ MeV}$. Assuming $r_{\text{nucl}} = 3 \times 10^{-5} \text{ \AA}$, $\Lambda_0 = 0.1 \text{ \AA}$ (corresponding to $\omega_0 = 320 \text{ THz}$) and $R_0 = 0.94 \text{ \AA}$ as the equilibrium spacing of two deuterons placed in *one site* in a hypothetical PdD₂ lattice, Schwinger estimated the fusion rate to be $\sim 10^{-19} \text{ s}^{-1}$ [5]. For a more realistic situation, with two deuterons in *two adjacent sites* of the PdD lattice, one has $R_0 = 2.9 \text{ \AA}$. Even assuming a lower value of $\omega_0 = 50 \text{ THz}$ corresponding to larger $\Lambda_0 = 0.25 \text{ \AA}$ [6], Eq. (2) will result in the fusion rate of $\sim 10^{-30} \text{ s}^{-1}$, which is too low to explain the observed excess heat generated in Pd cathode under D₂O electrolysis.

The above estimate is valid for the fusion rate between D–D or D–H ions in regular lattice sites. However, the ZPV amplitude can be increased locally under time-periodic modulation of the potential well width (that determines its eigenfrequency) at a frequency that exceeds the eigenfrequency by a factor of ~ 2 (*the parametric regime*). Such regime can be realized for a hydrogen or deuterium atom in metal hydrides/deuterides, such as NiH or PdD, in the vicinity of LAV [2,3]. Under parametric modulation, ZPV amplitude increases exponentially fast (Fig. 1a) with increasing number of oscillation periods $N = \omega_0 t / 2\pi$ [6]:

$$\Lambda_N = \Lambda_0 \sqrt{\cosh(g_\omega \pi N)}, \quad \Lambda_0 = \sqrt{\frac{\hbar}{2m\omega_0}}, \quad (3)$$

where $g_\omega \ll 1$ is the amplitude of parametric modulation, which is determined by the amplitude of LAV. For example, $g_\omega = 0.1$ corresponds to the LAV amplitude of $\sim 0.3 \text{ \AA}$ in the PdD lattice with $R_0 = 2.9 \text{ \AA}$, which is confirmed by molecular dynamic simulations of gap discrete breathers in NaCl type crystals [7]. Substituting Eq. (3) into the Schwinger Eq. (2) one obtains a drastic enhancement of the fusion rate with increasing number of oscillation periods N (Fig. 1b):

$$\frac{1}{T_N} \approx 2\pi\omega_0 \left(\frac{2\pi\hbar\omega_0}{E_{\text{nucl}}} \right)^{1/2} \left(\frac{r_{\text{nucl}}}{\Lambda_N} \right)^3 \exp \left[-\frac{1}{2} \left(\frac{R_0}{\Lambda_N} \right)^2 \right], \quad (4)$$

The parametric driving considered above requires rather special conditions similar to those in gap breathers in diatomic crystals [7], while in many other systems, e.g. in metals [12], oscillations of atoms in a discrete breather have different amplitudes but the same frequency. This case is closer to the driving of the potential well *positions* with the frequency equal to the potential eigenfrequency. Such driving does not increase the ZPV amplitude since the wave packet dispersion remains constant, however, the mean oscillation energy grows with time as [13]:

$$\langle E \rangle = \frac{\hbar\omega_0}{2} + \frac{g_x^2 \hbar\omega_0}{16} [\omega_0^2 t^2 + \omega_0 t \sin 2\omega_0 t + \sin^2 \omega_0 t], \quad (5)$$

where g_x is the relative amplitude of the position driving. Accordingly, one could expect an acceleration of the escape from a potential well of a finite depth similar to the parametric driving.

In reality, one is interested in the effect of potential well driving on the *tunneling* through the barrier of finite height between the wells as a function of the driving frequency and strength (amplitude). An analytical solution of the *non-stationary* Schrödinger equation even for the simplest case of a double well potential cannot be obtained. In the following section, we will analyze a *numerical solution* of Schrödinger equation for a particle in a double well potential, which is driven time-periodically imitating the action of a LAV or phason.

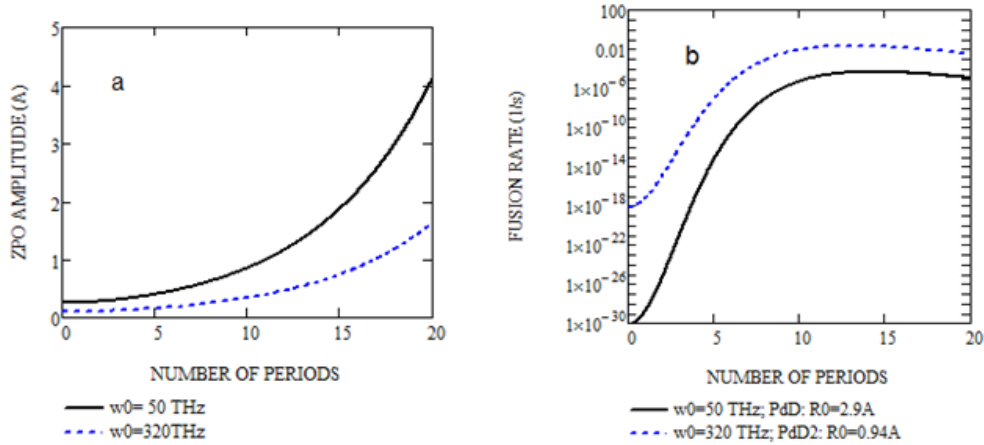


Figure 1. (a) Zero-point vibration amplitude of deuterium ions vs. N in the *parametric regime* [6] for different ω_0 according to Eq. (3) at $g = 0.1$. (b) D–D fusion rate $D-D \Rightarrow He^4 + 23.8 \text{ MeV}$ in PdD lattice according to Eq. (4) for deuterium ions in PdD lattice oscillating near equilibrium positions in one site ($R_0 = 0.94 \text{ \AA}$) or in two neighboring lattice sites ($R_0 = 2.9 \text{ \AA}$).

3. Tunneling in a Periodically Driven Double Well Potential

Consider the Schrödinger equation for a wave function $\psi(x, t)$ of a particle with a mass m in the non-stationary double-well potential $V(x, t)$:

$$i\hbar \frac{\partial}{\partial t} \psi(x, t) = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi(x, t) + V(x, t) \psi(x, t), \quad (6)$$

$$V(x, t) = \frac{m\omega_0^2}{2} \left[\frac{a(t)}{x_0^2} x^4 - b(t) x^2 \right], \quad x_0 = \sqrt{\frac{\hbar}{m\omega_0}}, \quad (7)$$

where $a(t)$ and $b(t)$ are the dimensionless parameters that determine the form and the driving mode of the potential shown in Fig. 2.

$$a(t) = \frac{1}{2\sqrt{\alpha}} [\alpha - \beta \cos(\Omega t)], \quad b(t) = \frac{1}{2\sqrt{\alpha}} \sqrt{\alpha - \beta \cos(\Omega t)}, \quad (8)$$

Ω is the driving frequency of the eigenfrequencies ω_{eigen} and positions x_{min} of the potential wells in the vicinity of the minima given by

$$\frac{\omega_{\text{eigen}}}{\omega_0} = \sqrt{2b} = \sqrt[4]{1 - \frac{\beta}{\alpha} \cos(2\omega_0 t)} \approx \left[1 - \frac{\beta}{4\alpha} \cos(2\omega_0 t) \right], \quad g_\omega = \frac{\beta}{2\alpha} \ll 1, \quad (9)$$

$$\begin{aligned} \frac{x_{\text{min}}}{x_0} &= \pm \sqrt{\frac{b}{2a}} = \pm \frac{1}{\sqrt{2}} \frac{1}{\sqrt[4]{\alpha - \beta \cos(2\omega_0 t)}} = \frac{1}{\sqrt{2}} \frac{1}{\alpha^{1/4} \sqrt[4]{1 - \frac{\beta}{\alpha} \cos(2\omega_0 t)}}, \\ &\approx \frac{x_{\text{min}}(0)}{x_0} \left(1 + \frac{\beta}{4\alpha} \cos(2\omega_0 t) \right), \quad g_x \equiv \frac{\beta}{4\alpha} \ll 1 \end{aligned} \quad (10)$$

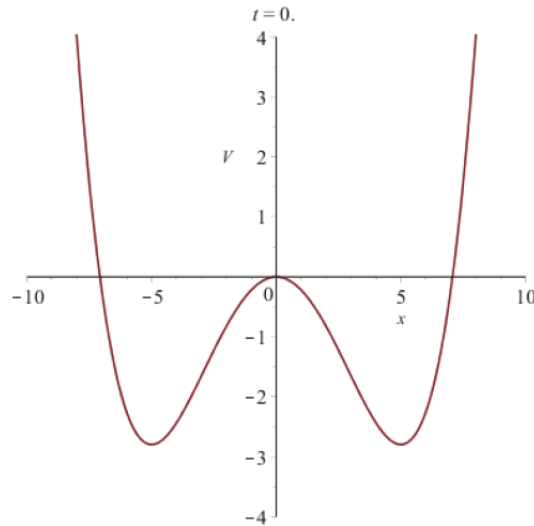


Figure 2. Double-well potential given by Eq. (7) at $\alpha = 0.0005$, $\beta = 0.0001$, which corresponds to the ratio of the potential depth to ZPV energy given by $1/8\sqrt{\alpha} \approx 5.6$.

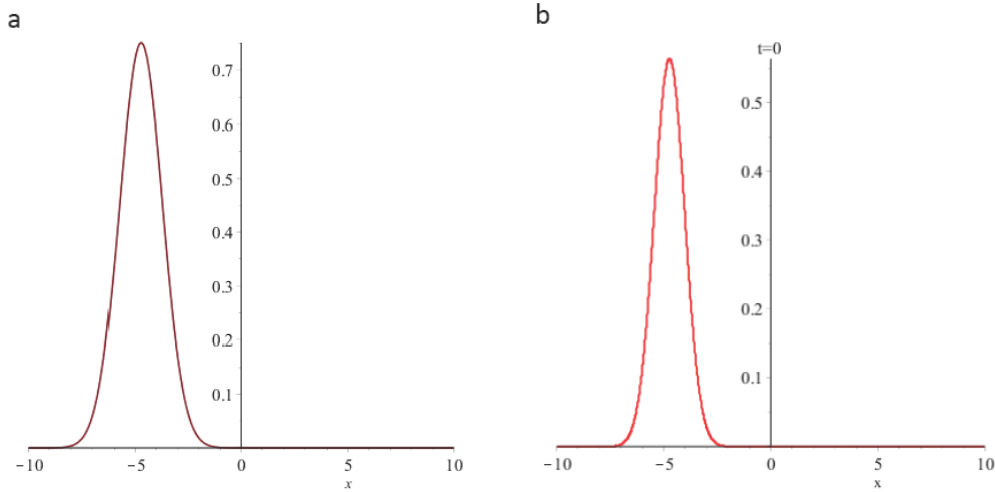


Figure 3. (a) Initial wave function $\psi(x, t_0 = 0)$ and (b) the probability distribution to find the particle at the point x : $\rho(x, t_0 = 0) = |\psi(x, t_0 = 0)|^2$ in the left potential well shown in Fig. 1.

From Eqs. (9) and (10) it follows that the driving under consideration results in a *simultaneous* time-periodic modulation of the potential well *positions* and *eigen frequencies* with amplitudes g_x and g_ω , respectively. Therefore, we are dealing here with a synergetic effect of the two mechanisms considered separately for a harmonic oscillator in the previous section and in [13].

Initial state of the system is described by a wave function of the Gaussian form placed near the first energy minimum (Fig. 2a):

$$\psi(x, t_0 = 0) = \frac{1}{\sqrt[4]{\pi x_0^2}} \exp\left(-\frac{(x - x_{\min})_0^2}{2x_0^2}\right). \quad (11)$$

The probability distribution of finding the particle at the point x is given by $\rho(x, t_0 = 0) = |\psi(x, t_0 = 0)|^2$, which is shown in Fig. 3b. It can be seen that the probability density is concentrated at $x_{\min} \approx 4.73$, which means the particle spends most of its time at the bottom of the potential well.

At the selected parameters, the potential depth to ZPV energy ratio is given by $1/8\sqrt{\alpha} \approx 5.6$, which is a typical ratio for solid state chemical reactions. This means that the particle energy is 5.6 times lower than the energy required to ‘jump’ over the barrier into another well. The mean time of tunneling through the barrier from a *stationary* potential well is very large, as can be seen from Fig. 4 showing the probability distribution of the particle at different moments of time $t = 2\pi/\omega_{\text{eigen}}$, measured in the oscillator periods. For example, $t = 1000$ corresponds to 1000 “attempts” to escape from the left well. However, one can see that the probability to find the particle in the right well is still negligibly small. Only at $t = 10\,000$, does it become higher than the probability to find the particle in the left well.

The situation becomes dramatically different in the case of time-periodically driven wells, as demonstrated in Fig. 5 for the two driving frequencies $\Omega = \omega_{\text{eigen}}; 2\omega_{\text{eigen}}$. In both cases, already at $t = 100$, the probability of finding the particle in the right well becomes comparable with the probability of finding the particle in the left well. This means that the mean escape (tunneling) time has decreased by ~ 2 orders of magnitude due to the driving with a comparatively small driving amplitude $g_\omega = 2g_x = 0.1 \ll 1$.

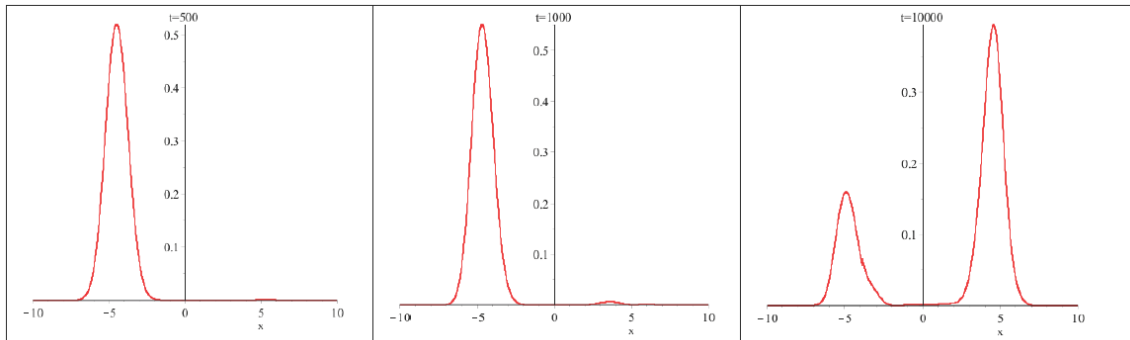


Figure 4. The probability distribution of the particle at different moments of time $t = 2\pi/\omega_{\text{eigen}}$ in stationary potential wells: $\alpha = 0.0005$; $\beta = 0$.

The driving frequency effect is different from that obtained for a harmonic oscillator [13], where two sharp peaks were observed at resonant frequencies $\Omega = \omega_{\text{eigen}}$ and $\Omega = 2\omega_{\text{eigen}}$. Due to a *simultaneous* time-periodic modulation of the potential well *positions* and *eigenfrequencies*, the accelerating effect of driving depends non-monotonously on the driving frequency with several maximums lying between ω_{eigen} and $2\omega_{\text{eigen}}$.

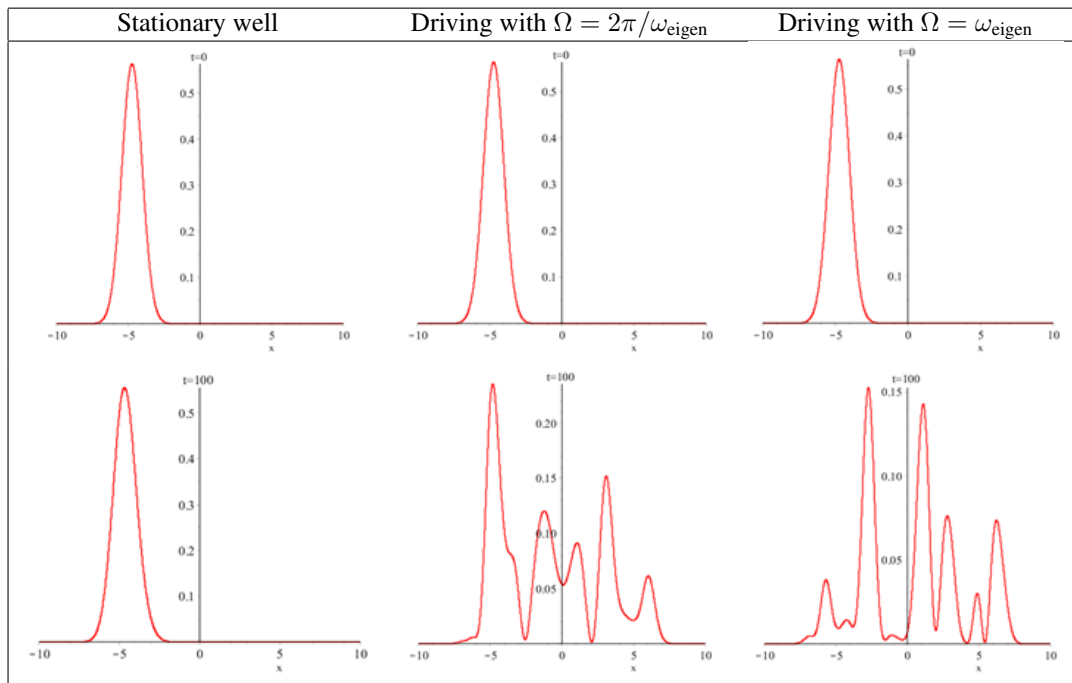


Figure 5. The probability distribution of the particle at different moments of time $t = 2\pi/\omega_{\text{eigen}}$ in stationary potential wells ($\alpha = 0.0005$; $\beta = 0$) and under the potential driving ($\alpha = 0.0005$; $\beta = 0.0001$) corresponding to $g_{\omega} = \beta/2\alpha = 0.1$; $g_x = \beta 4\alpha = 0.05$. The driving frequency Ω is indicated in the figure.

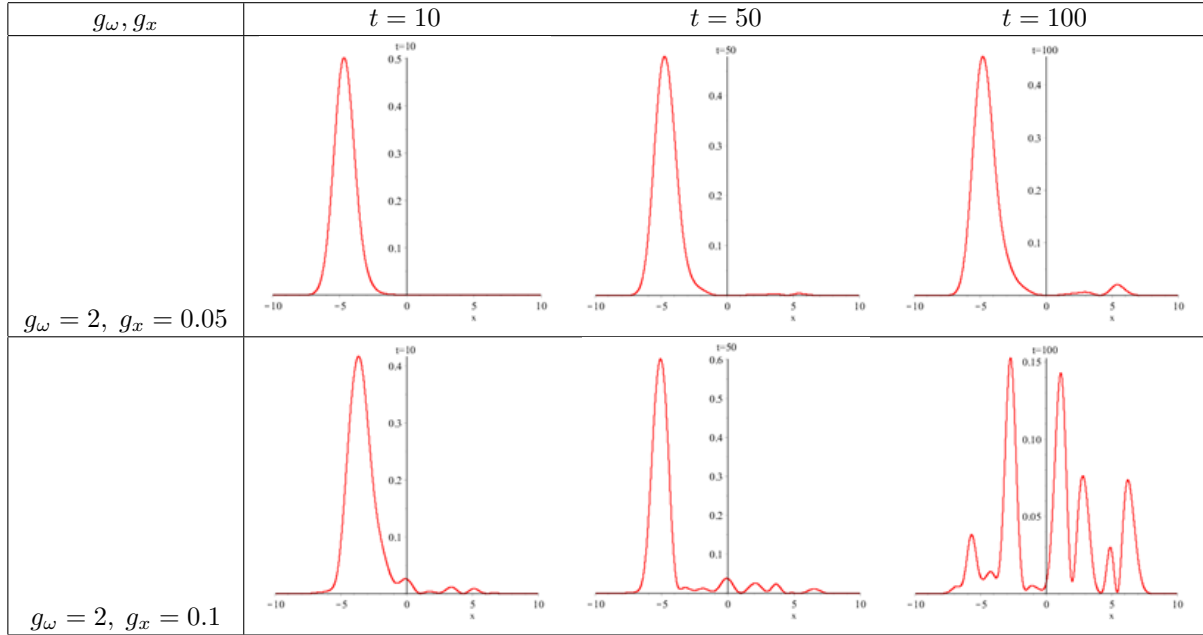


Figure 6. The probability distribution of the particle at different moments of time under the potential driving at $\Omega = \omega_{\text{eigen}}$, $\alpha = 0.0005$; $\beta = 0.00005 \div 0.0002$, corresponding to different driving amplitudes g_ω, g_x as indicated in the figure.

Finally, dependence of the tunneling time on the driving amplitude is shown in Fig. 6. It appears that increasing the amplitude by a factor of two results in decreasing the mean tunneling time by an order of magnitude. This example demonstrates the importance of the time-periodic driving of the potential wells in the vicinity of LAVs and phasons in the reactions involving quantum tunneling.

In the following section, we consider some characteristic examples of LAVs and phasons in quasicrystals.

4. LAVs and Phasons in Nanocrystals and Quasicrystals

The fact that the energy localization manifested by LAV does not require long-range order was first realized as early as in 1969 by Ovchinnikov, who discovered that localized long-lived molecular vibrational states may exist already in simple molecular crystals (H_2 , O_2 , N_2 , NO , CO) [14]. He realized also that stabilization of such excitations was connected with the *anharmonicity* of the intramolecular vibrations. Two coupled anharmonic oscillators described by a simple set of dynamic equations demonstrate this idea:

$$\begin{aligned} \ddot{x}_1 + \omega_0^2 x_1 + \varepsilon \lambda x_1^3 &= \varepsilon \beta x_2, \\ \ddot{x}_2 + \omega_0^2 x_2 + \varepsilon \lambda x_2^3 &= \varepsilon \beta x_1, \end{aligned} \quad (12)$$

where x_1 and x_2 are the coordinates of the first and second oscillator, ω_0 are their zero-point vibrational frequencies, ε is a small parameter, and λ and β are parameters characterizing the *anharmonicity* and the *coupling* force of the two oscillators, respectively. If one oscillator is displaced from the equilibrium and starts oscillating with an initial

amplitude, A , then the time needed for its energy to transfer to another oscillator is given by the integral:

$$T = \frac{\omega_0}{\varepsilon\beta} \int_0^{\pi/2} \frac{d\varphi}{\sqrt{1 - (A^2\gamma/4)^2 \sin^2 \varphi}}, \quad \gamma = \frac{3\lambda}{\beta}, \quad (13)$$

from which it follows that the full exchange of energy between the two oscillators is possible only at sufficiently small initial amplitude: $A^2\gamma/4 < 1$. In the opposite case, $A^2\gamma/4 > 1$, the energy of the first oscillator will *always be larger* than that of the second one. And for sufficiently large initial amplitude, $A \gg \sqrt{4/\gamma}$, there will be practically no sharing of energy, which will be localized exclusively on the first oscillator.

Thus, Ovchinnikov has proposed the idea of LAV for molecular crystals, which was developed further for any nonlinear systems possessing *translational symmetry*; in the latter case, LAVs have been named *discrete breathers* (DBs) or *intrinsic localized modes* (ILMs). Now, we are coming back to the idea of LAV arising at “*active sites*” in defected crystals, quasicrystals and nanoclusters. As noted by Storms, “Cracks and small particles are the Yin and Yang of the cold fusion environment”. A physical reason behind this phenomenology is that in topologically disordered systems, sites are not equivalent and band-edge phonon modes are intrinsically localized in space. Hence, different families of LAV may exist, localized at different sites and approaching different edge normal modes for vanishing amplitudes [9]. Thus, in contrast to perfect crystals, which produce DBs homogeneously, there is a *site selectiveness* of energy localization in the presence of spatial disorder, which has been demonstrated by means of atomistic simulations in biopolymers [9], metal nanoparticles [15] and, *experimentally*, in a decagonal *quasicrystal* $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$ [11].

The crystal shape of the nanoparticles (cuboctahedral or icosahedral) is known to affect their catalytic strength [16], and the possibility to control the shape of the nanoparticles using the amount of hydrogen gas has been demonstrated both experimentally by Pundt et al. [17], and by means of atomistic simulations by Calvo et al. [18]. They demonstrated that above room temperature the *icosahedral phase* should remain stable due to its higher entropy with respect to cuboctahedron. And icosahedral structure is one of the forms quasicrystals take, therefore one is tempted to explore further the *link between nanoclusters and quasicrystals*.

Figure 7 shows the structure of $\text{Pd}_{147}\text{H}_{138}$ cluster containing 147 Pd and 138 H atoms having minimum free energy configuration, replicated using the method and parameters by Calvo et al. [18]. In particular, Fig. 9(b) reveals the

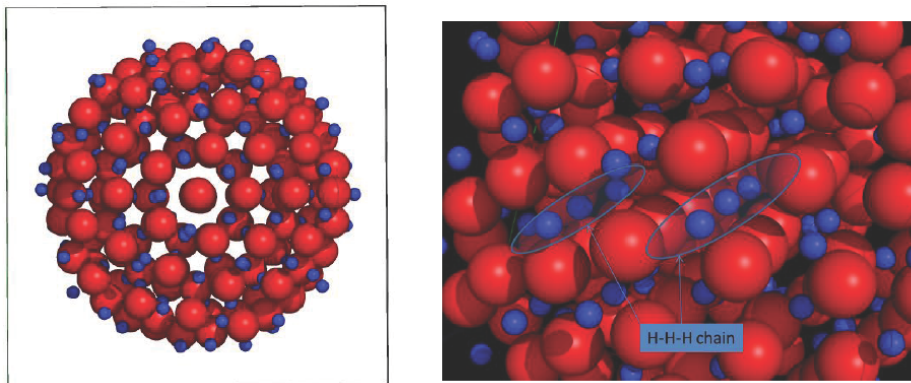


Figure 7. (Left) Structure of PdH cluster containing 147 Pd and 138 H atoms having minimum free energy configuration, replicated using the method and parameters by Calvo et al. [18]; (Right) H–H–H chains in the nanocluster, which are viable sites for LAV excitation [19].

presence of H–H–H chains aligned along the I -axis of the cluster. This ab initio simulation points out at the possibility of excitation of LAVs in these chains, with a central atom performing large-amplitude anharmonic oscillations and its neighbors oscillating in quasi-harmonic regime [19], which is similar to that considered in [7] for regular diatomic lattice of NaCl type. Such oscillations have been argued to facilitate LENR [2,3], and in the present paper we develop this concept further.

Let us consider phasons observed in a decagonal *quasicrystal* $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$ [11] and a possible link between LAVs and phasons.

Abe et al. [11] have measured by means of high resolution scanning transmission microscope (STEM) temperature dependence of the so-called Debye–Waller (DW) factor in decagonal *quasicrystal* $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$. DW factor is determined by the mean-square vibration amplitude of the atoms. The vibrations can be of thermal or quantum nature depending on the temperature. The authors demonstrated that the anharmonic contribution to Debye–Waller factor increased with temperature much stronger than the harmonic (phonon) one. This was the first *direct observation* of a “local thermal vibration anomaly”, i.e. LAVs, in our terms. The experimentally measured separation between LAVs was about 2 nm, which meant that their mean concentration was about 10^{20} per cm^3 that is many orders of magnitude higher than one could expect to find in periodic crystals [7].

The LAV amplitude dependence on temperature fitted by two points at 300 and 1100 K has shown that the maximum LAV amplitude at 1100 K = 0.018 nm (Fig. 8a). What is more, it appears that LAVs give rise to phasons at $T > 990$ K, where a phase transition occurs, and additional quasi-stable sites β arise near the sites α . The phason amplitude of 0.095 nm (Fig. 8b) is an *order of magnitude larger* than that of LAVs. Thus, on the one hand, the driving amplitude induced by phasons is larger than that by LAVs, but on the other hand, phason oscillations may be less time-periodic (more stochastic), which requires more detailed investigations of the driving stochasticity effect on tunneling, as discussed in the following section.

5. Discussion and Outlook

In the present paper, we presented a numerical solution to the Schrödinger equation for a particle in a *non-stationary* double well potential, which is driven *time-periodically* imitating the action of a LAV or a phason on the reaction

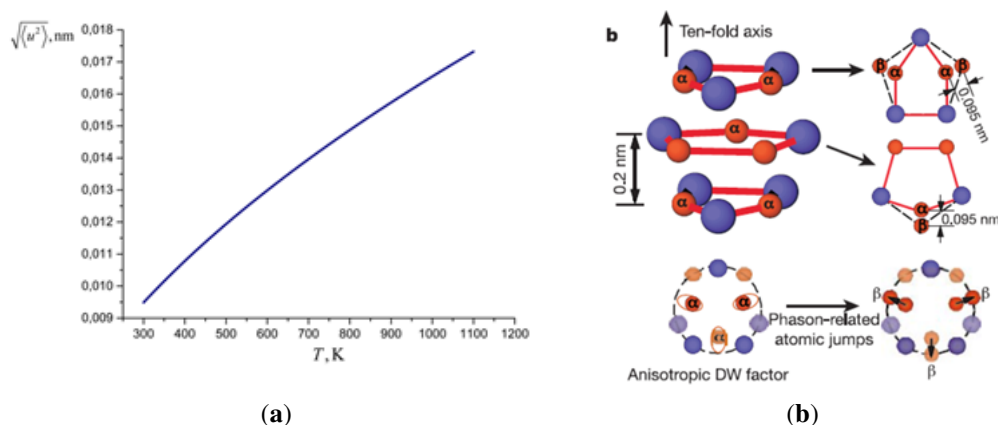


Figure 8. (a) LAV amplitude dependence on temperature in $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$, fitted by two points at 300 and 1100 K, according to Abe et al. [11]. The maximum LAV amplitude at 1100 K is 0.018 nm. (b) LAVs give rise to phasons at $T > 990$ K, where a phase transition occurs, and additional quasi-stable sites β arise near the sites α . The phason amplitude of 0.095 nm is an order of magnitude larger than that of LAVs.

cite in their vicinity. We have shown that the rate of tunneling of the particle through the potential barrier separating the wells can be enhanced by *orders of magnitude* with increasing number of driving periods. This effect is novel, since it differs qualitatively from a well-studied effect of resonance tunneling [20–22], a.k.a. Euclidean resonance (an easy penetration through a classical nonstationary barrier due to an under-barrier interference). In the latter case, the tunneling rate has a sharp peak as a function of the particle energy when it is close to the certain *resonant value* defined by the non-stationary field. Therefore, it requires a very specific parametrization of the tunneling conditions. In contrast to that, the time-periodic driving of the potential wells considered above, results, first of all, in a sharp and continuous (not quantum) increase of the ZPV amplitude and energy [6,13], which in its turn increases the tunneling rate. This result is closely related to the *correlation effects*, proposed by Dodonov et al. [23] and analyzed in details by Vysotskii et al. [24] who predicted a giant increase of sub-barrier transparency (up to hundreds of orders of magnitude) during the increase of the so-called *correlation coefficient* at special periodic action on a quantum system. This prediction was based on the numerical calculation of the time dependence of the correlation coefficient $r(t)$ for the case of a periodically driven *harmonic potential*, in which case it was shown that

$$|r(t)| \xrightarrow{t \rightarrow \infty} 1$$

at any *initial energy* of the oscillator, which was argued to result in a tunneling through the potential barrier of *any height* after sufficient number of driving periods. However, as shown more recently by Dubinko and Laptev [6], the oscillator energy also increases exponentially with time in the parametric regime considered in [24], which poses a limit to the correlation coefficient increase in a *double well* system (which is more relevant for the tunneling analysis than the infinite parabolic well considered in [6,24]).

As shown in the present paper, the tunneling probability increases strongly with increasing strength of the driving, which is related to the amplitude of the non-linear dynamic phenomenon that causes the driving. As we have demonstrated in the previous section, the driving amplitude induced by phasons may be larger than that induced by LAVs by an order of magnitude, which implies that phasons may be stronger catalysts than LAVs. However, further research is needed in order to make more definite conclusions, since the phason dynamics itself is an activated process driven by thermal or quantum fluctuations. Therefore, phasons can hardly induce a strictly time-periodic driving considered in the present paper. The tunneling rate through a fluctuating barrier in the presence of a periodically driving field has been shown to decrease with increasing fluctuation strength [25]. One may expect similar effects due to fluctuations in the cases of LAV and phason driven tunneling, which requires further investigation.

In conclusion, the present results support the concept of *nuclear catalysis* in QCs taking place at special sites caused by their inherent topology. This makes QCs a logical model to explain the structure of the microscopic nuclear active environments, or *hot-spots* observed by experimentalists in TEM analysis.

Acknowledgements

The authors would like to thank Dmitry Terentyev for designing Fig. 7 and Dan Woolridge – LAV animation [19]. VD and DL gratefully acknowledge financial support from Quantum Gravity Research.

References

- [1] V. I. Dubinko, *J. Condensed Matter Nucl. Sci.* **14** (2014) 87.
- [2] V. I. Dubinko, Quantum tunneling in gap discrete breathers, *Lett. Materials* **5** (2015) 97.
- [3] V. I. Dubinko, *J. Condensed Matter Nucl. Sci.* **19** (2016) 1–12.
- [4] J. Schwinger, *Z. Phys. D* **15** (1990) 221.

- [5] J. Schwinger, Nuclear energy in an atomic lattice, *The First Annual Conference on Cold Fusion*, University of Utah Research Park, Salt Lake City, Utah, National Cold Fusion Institute, 1990.
- [6] V. I. Dubinko and D. V. Laptev, *Lett. Materials* **6** (2016) 16.
- [7] L.Z. Khadeeva and S.V. Dmitriev, *Phys. Rev. B* **84** (2011)144304.
- [8] V. I. Dubinko, *J. Micromech. Mol. Phys.* **1** (2016) 165006.
- [9] V.I. Dubinko and F. Piazza, *Lett. Materials* **4** (2014) 273.
- [10] M. Yoshimura and A.P. Tsai, *J. Alloys Compound* **342** (2002) 451.
- [11] E. Abe, S.J. Pennycook and A.P.Tsai, *Nature* (London) **421** (2003) 347.
- [12] D. Terentyev, A. Dubinko, V. Dubinko, V. Dmitriev and E. Zhurkin, *Modelling Simul. Mater. Sci. Eng.* **23** (2015) 085007.
- [13] V.I. Dubinko, A.S. Mazmanishvili , D.V. Laptev and J. F. R.Archilla, *J. Micromech. Mol. Phys.* **1** (2016) 1650010.
- [14] A.A. Ovchinnikov, *Zh. Eksp. Teor. Fiz.* **57** (1969) 2137.
- [15] H. Zhang and J. F. Duglas, *Soft Matter* **9** (2013) 1266.
- [16] B. Corain, G. Schmid and N. Toshima (Eds.), *Metal Nanoclusters in Catalysis and Materials Science, The Issue of Size Control*, Elsevier , Amsterdam, 2008, p. 470.
- [17] A. Pundt, A. Dornheim, M. Guerdane, H. Teichler, H. Ehrenberg, M.T. Reetz and N.M. Jisrawi, *Eur. Phys. J. D* **19** (2002) 333.
- [18] F. Calvo and A. Carre, *Nanotechnol.* **17** (2006) 1292.
- [19] D. Woolridge, *Quantum Gravity Research*, Los Angeles, CA 90290, USA.
<https://www.dropbox.com/s/557akac5zoynqs/LAV%20animation%20in%20PdH%20cluster.mp4?dl=0>.
- [20] B.I. Ivlev and V. I. Melnikov, in *Quantum Tunneling in Condensed Media*, A. Leggett and Yu. Kagan (Eds.), NorthHolland, Amsterdam, 1992.
- [21] J.P. Palomares-Báez, B. Ivlev and J.L. Rodríguez-López, *Phys. Rev. A* **76** (2007) 052103.
- [22] B.I. Ivlev, *Phys. Rev. A* **66** (2002) 012102.
- [23] V.V. Dodonov, V.I. Man'ko, *Phys. Lett. A* **79** (2/3) (1980) 150.
- [24] V.I. Vysotskii and M.V. Vysotskyy, *Eur. Phys. J. A* (2013) . DOI 10.1140/epja/i2013-13099-2.
- [25] A. Saha and P. Sarkar, *Int. J. Quantum Chem.* **97** (2004) 914.